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Rotor Resistance Estimator based on Virtual Current Sensor Algorithm for Induction Motor Drives

Research Article

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Abstract: In this article, model reference adaptive system (MRAS)-based estimator of a rotor resistance of an induction motor (IM) is presented. In contrast to the solutions known from the literature, the reference model of this estimator uses the measured values of the phase current and the adaptive part is a virtual current sensor. The article presents an accurate description of the algorithm taking into account the discrete equations for possible practical implementation in the microprocessor system. In the first step, the impact of motor parameters to stator current estimation quality in the adaptive model was checked. Subsequently, simulation tests of the proposed rotor resistance estimator were carried out for the field-oriented control of the induction motor drive system with a model of an induction motor with fixed parameters and an induction motor with a changing main inductance according to a magnetisation curve. The analysis of the estimator's work showed its high efficiency and insensitivity to changes in the IM main inductance.

Keywords: induction motor drive • rotor resistance estimator • model reference adaptive system • virtual current sensor • fault tolerant control

Nomenclature

 $\Psi_{s}, \Psi_{r}, \Psi_{m}$ – spatial vectors of the stator, rotor and magnetic fluxes,

- spatial vectors of the stator, rotor and magnetic currents, **i**_s, **i**_r, **i**_m
- u_s - spatial vector of the stator voltage,
- electromagnetic and load torques, t_{em}, t_{L}
 - angular speed,
- ω" $I_m, I_{\sigma s}, I_{\sigma r}$ main, stator and rotor winding leakage inductances,
- the stator and rotor winding resistances. r_, r_

All state variables and parameters are expressed in per unit system [p.u.].

1. Introduction

In induction motor (IM) drives, precise control techniques belong to the group of vector methods (Orlowska-Kowalska and Dybkowski, 2016). The most popular ones are the direct torque control (DTC) and the direct rotor flux oriented control (DRFOC). There are difficulties in measuring state variables such as vectors of rotor flux Ψ_{r} and stator flux Ψ_{e} . These variables should be estimated (Dybkowski, 2018) based on measured signals.

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All model-based estimators of state variables use parameters of the IM. An accurate identification is very important to correct the operation of the IM drive system. However, the parameters are susceptible to change their values in time, according to a work point and temperature of the windings. Therefore, for increasing the efficiency of the IM drive systems, the use of estimators of the IM parameters is highly recommended.

The literature provides a detailed overview of methods for estimating the selected IM parameters (Toliyat et al., 2003). The techniques presented here can be divided into two groups: working online and offline.

Nowadays, many induction motors work with inverters produced by different companies. Therefore, it is usually necessary to determine the IM parameters before the target operation, which is done by offline identification. This way, by using, e.g. the idle-running and short-circuit tests the parameters of the IM equivalent scheme can be determined with a certain degree of accuracy. This solution allows the use of vector control methods, but in this case, it is assumed that the identified parameters are constant over the entire range of operation. Since the parameters change depending on many factors such as the change in the temperature of the windings or the changes in the drive operating point, this is not a precise solution but only sufficient.

To increase precision in IM control, online parameter estimation methods should be used. Such a solution allows us to estimate parameter values during the system operation. This is particularly important for systems that operate under conditions such as field weakening, where the main inductance changes. It should also be remembered that a long operation time has an impact on temperature changes in windings, and consequently, changes in the winding resistance values.

The rotor resistance is one of the IM parameters that significantly affect the accuracy of control and in particular the accuracy of estimation of motor state variables. This parameter can be estimated online based on various techniques, and is divided into four groups: spectral analysis techniques, observer-based techniques, Model Reference Adaptive System (MRAS)-Based Techniques and other methods.

Spectral analysis techniques uses the analysis of characteristic harmonics in measured values of stator currents and/or voltages (Zai et al., 1992; Loron and Laliberte, 1993). Among the observer-based techniques, the extended Kalman filters (EKF) (Barut et al., 2012; Zerdali and Barut, 2018; Horváth and Kuslits, 2018) and extended Luenberger observers (ELO) are popular (Orlowska-Kowalska, 1989; Du and Brdys, 1993). In the case of EKF, a problem with linearisation of the extended mathematical model of IM in each numerical step appears. Also, there are difficulties with the selection of Q and R, which are the covariance matrices. ELO is an analytic algorithm and thus its design is much simpler, and the number of calculations required for a given numerical step is disproportionately smaller.

MRAS techniques, based on the reference model and adaptive model are the most popular group. The adaptive model, as opposed to the reference model, utilises the estimated parameter. The aim of the system is the most accurate approximation to its real value so that the adaptive model has the same response as the reference model. MRAS techniques can be used to improve the performance of sate variables estimators and control algorithms. For example, the adaptive structure for the rotor resistance estimator, shown by (Zorgani et al., 2010) was used to improve the performance of the speed estimator MRAS^{CC} (Dybkowski and Orlowska-Kowalska, 2013).

Three methods of estimating the rotor resistance in an adaptive system are presented in Mapelli et al. (2012), based on active power, reactive power and torque, respectively. For all these methods, the sensitivity of the selected rotor resistance estimators to other IM parameters changes, and the correctness of operation at different operating points were tested. The authors have shown that the estimator based on reactive power is insensitive to load torque changes.

In Zorgani et al. (2019), a sensorless drive system with an induction motor operating at very low frequencies is presented. The MRAS type rotor resistance estimator used in this research is based on the relationship between current and voltage stator flux models. The authors demonstrated the stability conditions of the proposed rotor resistance estimator.

Many of the solutions concerning the estimation of the rotor resistance contained in the literature refer to the improvement of IM angular velocity estimation precision. In systems with a higher safety level, it is an alternative to the encoder in case of its damage. It should be mentioned that the current sensors are not reliable either. In the literature, a solution providing vector control of the drive system from the IM in case of loss of the information about measured stator phase currents is known (Adamczyk and Orlowska-Kowalska, 2019). However, also, in this case, precise knowledge of the rotor resistance value is important, because the identified errors worsen the quality of stator current reconstruction.

This article proposes a rotor resistance estimator, based on measured and estimated values of stator currents. This solution also improves the quality of current estimation in case of current sensor failure and is directed to current sensors fault-tolerant control (CS-FTC) systems.

2. Mathematical model of an induction motor

Following the generally accepted simplifications described among others in (Kazmierkowski et al., 2002; Orlowska-Kowalska, 2003) IM mathematical model can be presented using differential equations written in a stationary reference frame as follows (in p.u.):

voltage equation of the stator winding:

$$\frac{d}{dt}\Psi_s = \left(\mathbf{u}_s - r_s \mathbf{i}_s\right) \frac{1}{T_N},\tag{1}$$

voltage equation of the rotor winding:

$$\frac{d}{dt}\Psi_r = \left(\frac{r_r}{l_r}\left(l_m\mathbf{i}_s - \Psi_r\right) + j\omega_m\Psi_r\right)\frac{1}{T_N},\tag{2}$$

- flux-current equations:

$$\Psi_s = l_s \mathbf{i}_s + l_m \mathbf{i}_r, \tag{3}$$

$$\Psi_r = l_r \mathbf{i}_r + l_m \mathbf{i}_s,\tag{4}$$

- magnetic flux equation:

$$\Psi_m = \Psi_s + l_{\sigma s} \mathbf{i}_s, \tag{5}$$

where $I_s = I_{\sigma s} + I_m$, $I_r = I_{\sigma r} + I_m$, $T_N = 1/2\pi f_{sN}$ and f_{sN} – nominal frequency.

Equivalent circuit of the induction motor is shown in Figure 1.

The expression for the IM electromagnetic torque is as follows:

$$t_{em} = \operatorname{Im}\left(\Psi_{s}\mathbf{i}_{s}^{*}\right),\tag{6}$$

and the equation of motion is:

$$\frac{d}{dt}\omega_m = \left(t_{em} - t_L\right)\frac{1}{T_M},\tag{7}$$

where T_{M} – mechanical time constant of the drive.

The amplitude of the magnetising current can be represented by the following equation:

$$\mathbf{i}_m = \mathbf{i}_s + \mathbf{i}_r \,. \tag{8}$$

In a squirrel-cage IM, it is not possible to measure the rotor current, whereas an assumption (8) in a mathematical model makes the value of the main inductance constant over the whole range of motor operation. Therefore, in the



Fig. 1. Equivalent circuit of the induction motor

mathematical model used in the tests described in this article, an approximate form of the magnetisation curve was adopted, which affects the value of the main inductance I_m depending on the motor operating conditions. Under this assumption, the amplitude of the magnetising current depends on the amplitude of the magnetising flux:

$$\mathbf{i}_m = f\left(\Psi_m\right) = a\Psi_m + (1-a)\Psi_m^b,\tag{9}$$

where a = 0.7 and b = 7 are constants. The method of selecting these coefficients is described in more detail in Levi et al. (2000). Taking into account the above equation, the main inductance I_m , expressed in p.u., is a parameter depending on the magnetisation flux module Ψ_m according to:

$$l_m = \frac{\Psi_m / \Psi_{mN}}{i_m / i_{mN}} l_{mN} = \frac{\Psi_{mN}}{i_{mN}} l_{mN} \left(a + (1-a) \Psi_m^{b-1} \right)^{-1}.$$
 (10)

3. Structure of rotor resistance estimator

3.1. Virtual current sensor

The proposed rotor resistance estimator is based on the virtual current sensor (VCS) presented in Adamczyk and Orlowska-Kowalska (2019). This algorithm is based on equations (1), (2). It may be presented in a discrete form, in a stationary coordinate system (α - β) using the following equations:

$$i_{s\alpha}^{e}(k+1) = i_{s\alpha}^{e}(k) + \frac{1}{l_{s}\sigma} \left(u_{s\alpha}(k) - r_{s}i_{s\alpha}^{e}(k) - \frac{l_{m}}{l_{r}} \left(\frac{r_{r}}{l_{r}} \left(l_{m}i_{s\alpha}^{e}(k) - \Psi_{r\alpha}^{i}(k) \right) - \omega_{m}(k)\Psi_{r\beta}^{i}(k) \right) \right) \frac{T_{s}}{T_{N}}, \tag{11}$$

$$i_{s\beta}^{e}(k+1) = i_{s\beta}^{e}(k) + \frac{1}{l_{s}\sigma} \left(u_{s\beta}(k) - r_{s}i_{s\beta}^{e}(k) - \frac{l_{m}}{l_{r}} \left(r_{r} \left(l_{m}i_{s\beta}^{e}(k) - \Psi_{r\beta}^{i}(k) \right) + \omega_{m}(k)\Psi_{r\alpha}^{i}(k+1) \right) \right) \frac{T_{s}}{T_{N}},$$
(12)

whereby the components of the rotor flux vector are estimated based on the current rotor flux model (Orlowska-Kowalska, 2003):

$$\Psi_{r\alpha}^{i}(k+1) = \Psi_{r\alpha}^{i}(k) + \left[\frac{r_{r}}{l_{r}}\left(l_{m}i_{s\alpha}^{e}(k) - \Psi_{r\alpha}^{i}(k)\right) - \omega_{m}(k)\Psi_{r\beta}^{i}(k)\right]\frac{T_{s}}{T_{N}},$$
(13)

$$\Psi_{r\beta}^{i}(k+1) = \Psi_{r\beta}^{i}(k) + \left[\frac{r_{r}}{l_{r}}\left(l_{m}i_{s\beta}^{e}(k) - \Psi_{r\beta}^{i}(k)\right) + \omega_{m}(k)\Psi_{r\alpha}^{i}(k+1)\right]\frac{T_{s}}{T_{N}}.$$
(14)

This algorithm requires the measurement of the angular speed and the DC bus voltage u_{dc} in the voltage-source inverter (VSI) intermediate circuit. With the assumption that transistors of the VSI are considered as ideal switches, based on the discrete values of u_{dc} , the stator voltage vector components are calculated according to:

$$u_{s\alpha}(k+1) = \frac{2}{3}u_{dc}(k) \left(S_A(k) - \frac{1}{2} \left(S_B(k) + S_C(k) \right) \right), \tag{15}$$

$$u_{s\beta}(k+1) = \frac{\sqrt{3}}{3} u_{dc}(k) \left(S_B(k) - S_C(k) \right), \tag{16}$$

where S_A , S_B , S_C are logic states of VI connectors and $\sigma = I_m^2/I_s I_r$ - leakage factor of the motor. The flow chart of the VCS algorithm is shown in Figure 2.

As can be seen above, VCS uses the parameters of the IM equivalent circuit, i.e. rotor resistance r_r , stator resistance r_s , main inductance I_m , the leakage inductance of the rotor I_{or} and stator I_{os} windings. In the next subsection, the influence of correct identification of these parameters on the quality of stator current estimation was examined.

3.2. Impact of induction motor parameters on the quality of stator current estimation

The tests of the described VCS were carried out in MATLAB-Simulink environment using method ode1 with calculation step 6.25e-6, for the IM (mathematical model (1)-(7)) fed from VSI with ideal switches. The quality of stator current estimation was tested for 0.1s (5 periods of the fundamental frequency) for steady-state, rated speed, and 75% of rated torque. Figure 3 shows the waveforms of the i_{sa} measured (index *m*) and estimated (index *e*) stator current component in α axis, for different values of the rotor resistance. The test were carried out for constant nominal values of other IM parameters. The IM parameters are given in Table A1 in the Appendix.

The analysis of Figure 3b,c showed that the rotor resistance has a large impact on the estimation quality of the stator current. Changes in this parameter have the greatest impact on the current amplitude. On this basis, a quality indicator has been proposed using the difference in amplitudes of the measured and estimated stator current vectors:

$$e_{i} = \frac{1}{k_{2} - k_{1}} \sum_{j=k_{1}}^{k_{2}} \left| \mathbf{i}_{s}^{m}(j) - \mathbf{i}_{s}^{e}(j) \right|, \tag{17}$$

where: $k_1 = t_1/T_s$, $k_2 = t_2/T_s + 1$, T_s – sample time.

Table 1 shows the impact of IM parameters on this estimation quality indicator. The percentage value of the tested parameter is referred to as its rated value adopted in the IM model. For correctly identified parameters this index was equal to 0.0002.



Fig. 2. Flow chart of the VCS algorithm



Fig. 3. The measured and estimated current i_{sa} for $r_r = r_r^{IM}$ (a), $r_r = 0.75r_r^{IM}$ (b), $r_r = 1.25r_r^{IM}$ (c)

X/X ^N	ľ,	ľ _s	I _m	l or	l _{σs}
75%	0.1533	0.0102	0.1015	0.0069	0.0030
125%	0.1469	0.0104	0.0350	0.0074	0.0036





Fig. 4. The measured and estimated current i_{sa} for $l_m = 0.75 l_m^{M}$ (a), $l_m = 1.25 l_m^{M}$ (b)

The table above shows that not only the rotor resistance r_r (Figure 3) but also the main inductance I_m (Figure 4) has some impact on the quality indicator.

3.3. Rotor resistance estimator

The estimator of rotor resistance proposed in this article has a structure of an MRAS system. The adaptive part is the model of the virtual current sensor described in the previous subsection, while the reference part is the value of the measured phase current. The idea of this estimator is shown in Figure 5.

The output signal of the PI regulator in the above algorithm is the rotor resistance value (18), which is used for tuning the adaptive model (VCS) of the estimator:

$$r_r^e = k_{Pr} \left(\mathbf{i}_s^{m^*} - \mathbf{i}_s^{e^*} \right) + k_{Ir} \int \left(\mathbf{i}_s^{m^*} - \mathbf{i}_s^{e^*} \right) dt, \tag{18}$$

where: $k_{Pr'}$, k_{lr} – the gains of the proportional and integral part of the PI regulator.



Fig. 5. Scheme of the proposed rotor resistance estimator algorithm

To investigate the changes in amplitudes of the measured and the estimated stator current, which are the signals used in the rotor resistance estimator (Figure 5) in the drive system simulation model, the slow variations of the rotor resistance r_r^{M} , in the IM mathematical model has been assumed as shown in Figure 6. Besides, the identification error of the rotor resistance equal to 110% of its nominal value was assumed in the DRFOC control structure. Then the drive system was tested in the operating system as shown in Figure 7 (a - reference speed, b - load torque). The simulation results are shown in Figure 8.

Because of the small calculation step in simulation tests and the modulation effect of the VSI transistors the current signals (Figure 8a) are characterised by a certain degree of change in their values. Therefore, they were filtered with a first-order filter, with a time constant of 0.1s. As can be seen, the higher the value of the rotor resistance in the motor model, the lower will be the value of the measured current and the higher will be the value of the estimated current.



Fig. 6. Changes of rotor resistance in the IM model



Fig. 7. Operating conditions of the drive system: reference speed (a), load torque (b) changes



Fig. 8. Modules of measured and estimated stator current, before filtration (a), after filtration (b)

4. Rotor resistance estimator work analysis

As shown in Table 1, the quality of phase current estimation, apart from the rotor resistance r_r is also affected by the main inductance I_m . Besides, temperature changes in windings can affect not only the rotor resistance but also the stator resistance. Because of this, the impact of r_s was checked too. Therefore, the tests of the proposed rotor resistance estimator were divided into two stages:

- 1 analysis at a constant value of main inductance, where a mathematical model of IM with commonly used simplifications is assumed,
- 2 analysis at a variable value of main inductance, where the variability of l_m according to equation (10) is assumed.

The tests have been conducted without and with changes of stator resistance and were carried out for the rotor speed and load torque changing as shown in Figure 7. In both cases, the rotor resistance estimator started working in the 3rd second. The changing of stator resistance started in the 5th second from nominal to 140% of nominal value, as shown in Figure 9.

All tests were carried out in the DRFOC structure shown in Figure 10. It should be mentioned here, that ideal switches have been taken in the simulation model of VSI.



Fig. 9. Changes in the stator resistance during simulation tests



Fig. 10. DRFOC structure with virtual current sensor and rotor resistance estimator: switch P in position 1 – classical control structure; switch P in position 2 – fault-tolerant control (FTC) structure

4.1. Analysis in the case of a constant value of the main inductance

Under the assumed operating conditions, the quality of rotor resistance estimation in the DRFOC system with a constant value of the main inductance was checked. The obtained results are shown in Figures 11-14 (a – test without, and b – with changing stator resistance).

It can be seen in Figure 11a that after switching on the estimator in the third second, the rotor resistance correctly follows the value adopted in the motor model for the constant value of stator resistance. Besides, this change is correctly tracked as it grows. For the test with changeable stator resistance (Figure 11b) the estimation error of the rotor resistance increases, however it is lower than 5% (see Figure 14b). It can be noticed in Figure 12 that the signals entering the estimator overlap, which is connected with the improvement of the stator current estimation quality due to rotor resistance estimation (Figure 13). When the rotor resistance estimator is switched on, both the errors of estimating the stator current are going to zero value independently of the stator resistance value. As it was said above, the rotor resistance estimation error goes to zero value for constant stator resistance (Figure 14a) and reaches close to 5% for the stator resistance changed up to 140% of its nominal value, as shown in Figure 14b.



Fig. 11. Rotor resistance in IM model and estimated one for I_m = const: test without changing r_s (a), with changing r_s (b)



Fig. 12. Signals used in estimator for $I_m = \text{const:}$ test without changing r_s (a), with changing r_s (b)



Fig. 13. Zoomed measured and estimated stator current i_{sa} for I_m = const: test without changing r_s (a), with changing r_s (b)



Fig. 14. Estimation errors of rotor resistance and stator current for $l_m = \text{const:}$ test without changing r_s (a), with changing r_s

4.2. Analysis in the case of a variable value of the main inductance

The next stage of the research was to check the quality of rotor resistance estimation assuming a variable value of the main inductance, under the same operating conditions as before. The magnetising curve modelled according to (10) is shown in Figure 15, while the changes of I_m during operation of the drive system, compared to its nominal value, can be seen in Figure 16. Also in this case the tests were carried out for constant and changeable stator resistance value. The results of the obtained tests are presented in Figures 17–20.

The above-mentioned transients show that also in the case of the IM mathematical model with magnetisation curve taken into account, the rotor resistance is estimated accurately according to the proposed algorithm for the



Fig. 15. Magnetisation curve



Fig. 16. Main inductance: test without changing r_s (a), with changing r_s (b)

test without changing r_s (Figure 17a). When the stator resistance is changing, the rotor resistance estimation error is a bit bigger than 5% (Figure 20b). The current signals used in the rotor resistance estimator coincide (Figure 18), which also indicates an improvement of the stator current estimation quality (Figure 19). It should be also mentioned that the estimation errors of the stator current are close to zero for constant and changeable stator resistance, however, the rotor resistance estimation error reaches around 5% in the case of stator resistance increased to 140%, as can be seen in Figure 20b.

As it results from the simulation tests carried out, the rotor resistance estimation is somewhat sensitive to changes in r_s . However, it seems that its simultaneous estimation does not make sense because these errors in the estimation the rotor resistance of a few percent do not affect the quality of the current estimation.



Fig. 17. Rotor resistance in IM model and estimated one for $I_m = var$: test without changing r_s (a), with changing r_s (b)







Fig. 19. Zoomed measured and estimated stator current i_{sa} for l_m = var: test without changing r_s (a), with changing r_s (b)



Fig. 20. Estimation errors of rotor resistance and stator current for l_m = var: test without changing r_s (a), with changing r_s (b)

5. Conclusions

The studies have shown that the developed rotor resistance estimator also works properly in a drive system model with a non-linear relationship between the flux and the magnetising current of the IM. Given the situation when the stator resistance is also changing (40% more than its nominal value), the estimation error of the stator current was close to zero while the rotor resistance error was around 5%. This is not a significant obstacle, as the accuracy of the identification of the IM parameters is evaluated at around 10%. Furthermore, the estimator of the rotor resistance helps to significantly improve the quality of the VCS regardless of the r_s changes, and it can be used in the VCS algorithm to improve its performance. For example, in the failure-free operation of the IM drive, the estimated rotor resistance r_r can be used in the current model of rotor flux. As the rotor resistance is a parameter with a low dynamics of change after the failure of the phase current sensors (when the proposed estimator cannot work) the average value r_r from the last second before the drive reconfiguration can be adopted to the VCS algorithm. This solution will ensure a better quality of CS-FTC operation (switch *P* from Fig. 10 in position 2). This issue will be the subject of further research.

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Appendix A

Table A1. Rated parameters of IM tested in simulation

Parameter	[ph.u.]	[p.u.]
Rated phase voltage U_N	230 V	0.707
Rated phase current I_N	2.5 A	0.707
Rated power P_N	1.1 kW	0.638
Rated speed n _N	1390 rpm	0.927
Rated frequency f _{sN}	50 Hz	1.0
Number of pole pairs p_{b}	2	_
Rotor winding resistance R,	5.064 Ω	0.550
Stator winding resistance R _s	5.114 Ω	0.556
Rotor leakage inductance $L_{\sigma r}$	31.6 mH	0.1079
Stator leakage inductance $L_{\sigma s}$	31.6 mH	0.1079
Main inductance L _m	478 mH	1.6323
Mechanical time constant $T_{_M}$	0.25 s	_
Rated rotor flux $\Psi_{_{N}}$	0.7441 Wb	0.7187
Rated stator flux $\Psi_{_{SN}}$	0.8235 Wb	0.7954
Rated magnetic flux $\Psi_{_{mN}}$	0.7518 Wb	0.7261